Ferroelectric transition under hydrostatic pressure in poly(vinylidene fluoride-trifluoroethylene) copolymers

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A clear ferroelectric transition of first-order type is observed in poly(vinylidene fluoride-trifluoroethylene) (P(VDF-TrFE)) random copolymers with TrFE contents higher than 20% and lower than 40%. This structural phase transition which takes place in the crystalline regions of the polymeric material has been analysed using neutron diffraction under hydrostatic pressure for three copolymer compositions: 80/20, 70/30 and 60/40. The $P-T$ phase diagrams have been determined in the ranges 0.1-300 MPa, 300-500 K both upon heating and upon cooling, and several thermodynamic parameters have been evaluated for the different crystalline phases: compressibility and thermal expansion coefficients, enthalpies of transition, etc. For the middle composition (70/30) the ferroelectric transition temperature T_c is well separated from the melting temperature T_m of the paraelectric phase and both transition temperatures increase with increasing pressure: $d\overline{T}_C/dP = 0.38$ K MPa⁻¹ and $d\overline{T}_m/dP = 0.25$ K MPa⁻¹. For the 80/20 composition the Curie temperature T_c is closer to the melting temperature T_m , and under increasing pressure the two transition lines are expected to merge at a triple point $(P^* \approx 500 \text{ MPa}, T^* \approx 560 \text{ K})$, above which a single line corresponds to the melting of the ferroelectric phase. For the 60/40 composition a new 'low temperature disordered' phase appears and coexists with the ferroelectric phase but with a volume fraction which depends on temperature and thermal history.

(Keywords: VDF-TrFE copolymers; semi-crystalline polymers; ferroelectric phase transition)

present, copolymers of vinylidene fluoride (VDF) and alternatively, Tashiro *et al.⁵* have proposed an intermediate trifluoroethylene (TrFE) have attracted much scientific the secoled the 'cooled phase' consisting of a k trifluoroethylene (TrFE) have attracted much scientific phase called the 'cooled phase' consisting of a kind of and technological research because of their piezoelectric micro-twinning of the small ferroelectric crystals and technological research because of their piezoelectric micro-twinning of the small ferroelectric crystals.
and pyroelectric effects¹. The effects of bydrostatic pressure have alreaded

in an amorphous matrix and this feature confers to the investigations have been performed on a macroscopic performed on a macroscopic performed on a macroscopic material a 'composite' microstructure^{2,3}.

As with other ferroelectric crystals these copolymers thermal analysis⁸ and ferroelectric hysteresis curves exhibit a ferroelectric-paraelectric transition which has thus mixing the contributions of the amorphous and exhibit a leffoelectric-paraelectric transition which has thus mixing the contributions of the amorphous and been clearly observed for VDF contents ranging from 65

In these copolymers the ferroelectric transition
temperature is strongly dependent upon the dipolar The temperature is strongly dependent upon the dipolar The present work was undertaken in order to analyse
energy which is responsible for the stability of the thermodynamic properties of the ferroelectric and energy which is responsible for the stability of the the thermodynamic properties of the ferroelectric and ferroelectric and ferroelectric and the thermodynamic properties of the ferroelectric and ferroelectric pressure Ferroelectric order and which decreases both with the paraelectric crystalline phases under hydrostatic pressure
VDF content⁶ and after electron or γ -ray irradiation⁷. For different contents of VDF. Neutron diffrac VDF content and after electron or γ -ray irradiation content contents of VDF. Neutron diffraction The characteristics of these copolymers are also very experiments permit the use of beaux vessels like high The characteristics of these copolymers are also very experiments permit the use of heavy vessels like high sensitive to thermal treatments³, mechanical orientation sensitive to thermal treatments⁻, mechanical orientation pressure cells, cryostats, etc. and are therefore well suited
and electrical poling², which affect the microstructure for the determination of phase diagrams and

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INTRODUCTION low temperature phase is not completely understood: Lovinger *et al.*⁴ have reported the coexistence of Among the few ferroelectric polymers known at a ferroelectric phase with a disordered helical phase;
present, copolymers of vinylidene fluoride (VDF) and alternatively Tashino et al.⁵ have proposed an intermediate

and pyroelectric effects.

In these materials, the crystalline lamellae, which

tudied by several methods mainly in conclumers with In these materials, the crystalline lamellae, which studied by several methods, mainly in copolymers with represent more than 60% of the volume, are embedded VDF contents lower than $60\%^{8-12}$. Most of these polymeric material a composite microstructure $\frac{1}{3}$. scale, e.g. dielectric measurements $1^{0,11}$, differential thermal analysis⁸ and ferroelectric hysteresis curves⁹ been clearly observed for VDF contents ranging from 65 crystalline regions. Only a few studies, based on X-ray
to 80%^{4,5}. differentially differentially contract the expectations diffraction^{8,12}, provide information on the crystalline

and electrical poling, which affect the microstructure for the determination of phase diagrams and for studies
and the degree of crystallinity. a different of the evolution of the lattice parameters *versus*
For less than 65% VDF content, the structure of the *temperature* and pressure These allow the determination temperature and pressure. These allow the determination of the compressibility and the thermal expansion of the crystalline phases and the volume change of the unit cell * To whom correspondence should be addressed through the ferroelectric transition.

P(VDF-TrFE) copolymers of compositions 70/30, 80/20 in each acquisition. and 60/40 mol% supplied by Atochem, France. From gel permeation chromatography (g.p.c.) all the samples had *Isothermal pressure scans.* The pressure was varied in approximately the same molecular weight $M_n \approx 100,000$ steps smaller than 30 MPa close to the ferroelectric and the same polydispersity index $\overline{M_w/M_n} \approx 2$. Moreover,
transition and larger than 30 MPa out of the transition
the microstructural data, obtained by high resolution the microstructural data, obtained by high resolution region. After each pressure step two successive acquisitions n.m.r., confirmed the randomness of the monomer of 10 min were performed but only the second n.m.r., confirmed the randomness of the monomer of 10 min were performed but only the second distribution¹³.

The raw material was melted in a cylindrical vanadium system reach quasi-equilibrium conditions. The average container of 40 μ m wall thickness almost transparent to rate of pressure change 1.5 MPa min⁻¹, was chosen t container of 40 μ m wall thickness almost transparent to rate of pressure change, 1.5 MPa min⁻¹, was chosen to neutrons (5 mm in diameter and 20 mm in length). Such produce the ferroelectric transition at a rate compa neutrons (5 mm in diameter and 20 mm in length). Such produce the ferroelectric transition at a rate comparable
a preparation is considered to have no effect on the temperature scan i.e. 0.5 K min⁻¹ (see below; the a preparation is considered to have no effect on the to the temperature scan, i.e. 0.5 K min^{-1} (see below; the orientation of the sample (isotropic powder symmetry change in the Curie temperature induced by pressure wa maintained). For each composition all the measurements of the order of $0.35 \text{ K} \text{ MPa}^{-1}$. were carried out with the same specimen.
Before conducting the sequence of measurements a

Before conducting the sequence of measurements a *Effects of the phase transitions on the diffractograms* pressure cycle, up to 300 MPa and back to atmospheric pressure cycle, up to 300 MPa and back to atmospheric *Figure 1* shows three typical diffraction patterns pressure, and a temperature cycle, up to the paraelectric phase and back to room temperature, were carried out phase and back to room temperature, were carried out
in order to remove any possible residual stress in the ferroelectric phase, in the

Laue-Langevin on the high flux powder diffractometer diagram, only the Q range between 1 Å^{-1} and 1.6 Å^{-1}
D20. A graphite monochromator ((002) reflection) was analyzed (with the multidatestar in a fixed negitio D20. A graphite monochromator $((002)$ reflection) was analysed (with the multidetector in a fixed position) provided a neutron beam of wavelength 2.41 Å defined for three complementary reasons: (i) the most obvious to within 0.01 Å. The precise wavelength and the angular position of the incident beam were calibrated using a silicon powder standard. The beam size and the resolution were determined by the natural divergence of the beam (10 mrad) and by diaphragms positioned between the $\sqrt{300 \text{ K}}$ monochromator and the sample $(10 \text{ mm} \times 20 \text{ mm})$.

The instrument D20 is equipped with a multielectrode, position sensitive 3 He detector which covers an angular $\left| \right|$ (110.200) range of 12.6° (126 channels) and can be moved step by step around the sample axis to cover wider angular ranges. The channel sensitivities were calibrated with an isotropic incoherent scatterer (vanadium). In order to reduce parasitic scattering and to protect the detector
from receiving the direct beam, additional cadmium
screens and slits were positioned along the beam path.
Sample environment
The sample container was placed in a pre from receiving the direct beam, additional cadmium screens and slits were positioned along the beam path. $\dot{\mathbf{S}}$ / (310,020) (320,400) (310,020) (220,400)

__I/ *Sample environment*

made of a copper-beryllium alloy which allows pressures \mathbf{F} | 380 K | (310,020) of up to 300 MPa and temperatures of up to 500 K¹⁴. \sum_{μ} | $\left| \begin{array}{ccc} | & | & | \end{array} \right|$ (220,400) (001) Helium gas was used for transmitting the pressure from the compressor to the sample chamber. The pressure was measured outside the vessel with a manganese gauge having an accuracy of about 2%. C

The pressure cell was placed in a cryo-furnace (1.5-600 K) whose temperature regulation was ensured by an analog controller. The temperature of the pressure cell was measured using a rhodium-iron resistor.

The measurements were carried out in two different $Q(\hat{A}^{-1})$ ways.

with continuous slow heating and subsequent cooling. A (425 K). The three plots are shown with the same scales

EXPERIMENTAL rate of about $0.5 K min^{-1}$ was chosen in order to get a good temperature homogeneity and to avoid any kinetic Samples
The samples used in this study were random
The samples used in this study were random
Smin a temperature range of about 2.5 K was covered 5 min , a temperature range of about 2.5 K was covered

distribution¹⁹.
The raw material was melted in a cylindrical vanadium and the system reach quasi equilibrium conditions. The average change in the Curie temperature induced by pressure was

recorded during a heating run at ambient pressure paraelectric phase and in the molten state. These specimen.
diffractograms, over a broad Q range, have been obtained *Neutron diffraction instrument* **by** scanning the angle of the multidetector in steps of 3° and regrouping the data into a single file. For The experiments were performed at the Institut the determination of the pressure-temperature phase
Laue-Langevin on the high flux powder diffractometer diagram only the Ω range between $1 \stackrel{\delta}{A}^{-1}$ and $16 \stackrel{\delta}{A}^{-1}$ for three complementary reasons: (i) the most obvious

Figure 1 Neutron powder diffractograms of the 70/30 copolymer (during a heating run at ambient pressure): (a) in the ferroelectric phase *Isobaric temperature scans.* These were performed (300 K); (b) in the paraelectric phase (380 K); (c) in the molten phase

ិទ

changes through the two phase transitions are observed No special constraint in the least-squares procedure was around $Q = 1.3 \text{ Å}^{-1}$; (ii) the scanning procedure takes a imposed. around $Q = 1.3~\text{\AA}^{-1}$; (ii) the scanning procedure takes a much longer time; and (iii) spurious diffraction from the In the pseudo-hexagonal ferroelectric phase *(Figure 2c)* high pressure cell was also observed for $Q > 2.5 \text{ Å}^{-1}$. the asymmetry of the Bragg peak is mainly due

the three copolymers at ambient pressure has been double Lorentzian peak $(L_{110} + L_{200})$ was used for profile reported elsewhere¹⁵.

$Data$ *analysis*

For refining the positions and the intensities of the Bragg peaks, especially in the transition region, where both the ferroelectric and the paraelectric phases coexist, we used a program named 'CURFIT'¹⁶. This program we used a program named 'CURFIT'. This program where the parameters k and q were fixed according to is based on a least-squares fit by linearization of the structural data presented in ref. 15 (e.g. $k=0.5$ and fitting function. Empirically we found that, in the $q=0.018 \text{ Å}^{-1}$ for the copolymer of composition 70/30). Q range $1.0-1.6 A^{-1}$, the shapes of the ferroelectric and This procedure was chosen in order to limit the number paraelectric Bragg peaks were better described by a of fitted parameters, especially in the temperature range
Lorentzian function than by a Gaussian. Indeed, as is of phase coexistence (Figure 2b) where the diffraction Lorentzian function than by a Gaussian. Indeed, as is of phase coexistence *(Figure 2b)*, where the diffraction usual in semi-crystalline polymers, broad Bragg peaks natural parameters and a formal production usual in semi-crystalline polymers, broad Bragg peaks patterns were fitted with a paraelectric and a ferroelectric were observed due to the very small size of the coherent peak chosen as described above. When only the were observed due to the very small size of the coherent peak chosen as described above. When only the crystalline regions, and hence the shapes of the Bragg ferroelectric phase is present in the sample it is clear from crystalline regions, and hence the shapes of the Bragg ferroelectric phase is present in the sample it is clear from peaks are mainly determined by the size distribution of $F_{i \alpha \mu}$ and ϵ that the double I original peaks are mainly determined by the size distribution of *Figure 2c* that the double Lorentzian $L_{110} + L_{200}$ (broken
the crystallites.

In the hexagonal paraelectric phase the rather around 1.33 Å^{-1} attributed to the amorphous phase.
narrow Bragg peak was fitted with a single Lorentzian Alternatively a fit including a paraelectric peak (full line) narrow Bragg peak was fitted with a single Lorentzian Alternatively, a fit including a paraelectric peak (full line)
converges towards a non-zero intensity at the same characterized by its position Q_1 , its integrated intensity converges towards a non-zero intensity at the same
 I_1 and its full width at half maximum ΔQ_1 (Figure 2a). Solution Owing to this ambiguity the results o

gh pressure cell was also observed for $Q > 2.5 \text{ Å}^{-1}$. the asymmetry of the Bragg peak is mainly due to the A detailed analysis of the complete diffractograms of splitting of the reflections (110) and (200)¹⁵. Hence a A detailed analysis of the complete diffractograms of splitting of the reflections (110) and (200)¹⁵. Hence a the three copolymers at ambient pressure has been double Lorentzian peak ($L_{110} + L_{200}$) was used for profi fitting with parameters constrained in the following way

$$
I_{200} = kI_{110}
$$

\n
$$
Q_{200} = Q_{110} - q
$$

\n
$$
\Delta Q_{110} = \Delta Q_{200}
$$

the structural data presented in ref. 15 (e.g. $k=0.5$ and

e crystallites.
In the hexagonal paraelectric phase the rather $\frac{1}{2}$ around 1.33 λ ⁻¹ attributed to the amorphous phase position. Owing to this ambiguity, the results of this last fitting procedure were discarded when the intensity of the paralectric peak was smaller than 20% of its maximum value.

The diffraction pattern of the molten phase *(Figure lc)* $\frac{430 \text{ K}}{20 \text{ K}}$ $\frac{430 \text{ K}}{20 \text{ K}}$ the scattering function of the amorphous phase at any temperature since it appears that the line shape and the position of the amorphous halo change when the crystalline regions undergo a phase transition³. Moreover, owing to the large width of the halo $(\Delta Q > 0.3 \text{ A}^{-1})$, it cannot be adequately fitted in the restricted Q range investigated. A reliable description of the amorphous halo is thus difficult to establish from the the amorphous halo is thus difficult to establish from the
data presented here. Therefore, to simplify the fitting
procedure in the restricted Q range of interest, both the
incoherent scattering and the coherent scattering procedure in the restricted Q range of interest, both the $\begin{array}{ccc}\n\sqrt{21 \text{ K}}\n\end{array}$ $\begin{array}{ccc}\n\end{array}$ b incoherent scattering and the coherent scattering from the amorphous phase were accommodated using a the amorphous phase were accommodated using a straight background whose level and slope were fitted parameters.

Figure 2 displays examples of experimental data \mathbf{I} is the intervention of the fitted curves. Even if the agreement is $\frac{1}{\sqrt{2}}$ not fully satisfactory for individual sets of data, it must be emphasized that the aim of this treatment was to analyse series of diffractograms (approximately 600 for each composition) in order to observe *changes* induced by pressure and temperature. Therefore, although the simplified fitting procedure chosen may introduce systematic errors in absolute position, intensity or width of the Bragg peaks, we consider that it is accurate in 1.2 1.3 1.4 1.5 revealing *relative* changes in these quantities.

398 K

Figure 3 Series of neutron powder diffractograms of the 70/30 copolymer at 30 MPa in the Q range 1.1–1.55 Å⁻¹: (a) cooling run from 425 K to 335 K; (b) heating run from 340 K to 430 K

pattern, at 30 MPa, during a heating and cooling run. \vec{r} \vec{r} \cdots \vec{r} \cdots \vec{a}

Figure 3 shows the evolution of the powder diffraction
ttern, at 30 MPa, during a heating and cooling run.
The first diffraction pattern of *Figure 3* (bottom) reveals
about $Q = 1.4 \text{ Å}^{-1}$ the composite Bragg reflecti The first diffraction pattern of *Figure 3* (bottom) reveals $\dot{\mathbf{S}}$ 160 at about $Q = 1.4 \text{ Å}^{-1}$ the composite Bragg reflection $(200 + 110)$ of the ferroelectric phase and, near $\overline{Q} = 1.3 \text{ Å}^{-1}$, $\overline{Q} = 1.3 \text{ Å}^{-1}$, $\overline{Q} = 1.20$ a low intensity peak corresponding to the appearance of the paraelectric phase. As the temperature is raised a $\frac{\mu}{2}$ 80 transformation from ferroelectric to paraelectric phase gradually takes place and is completed at 395 K. Upon $\frac{1}{2}$ 40 further heating, the intensity of the paraelectric peak remains almost constant over 20 K and finally decreases

It is worth noting that, for this composition, the ferroelectric transition and the melting are clearly separated, the ferroelectric peak vanishing completely before the paraelectric peak starts to decrease.

If we now examine the cooling run from the molten

ate (*Figure 3*, top), we observe that the polymer

ystallizes rapidly and that the paraelectric phase

mains stable over a much wider range of temperatures

bout 50 K), state *(Figure 3, top)*, we observe that the polymer \vec{S} 160 crystallizes rapidly and that the paraelectric phase remains stable over a much wider range of temperatures (about 50 K), the ferroelectric transition taking place $\frac{1}{20}$ 120 below 355 K. $\mathbf{H} \circ \mathbf{S} = \mathbf{B} \circ \mathbf{S} + \mathbf{S} \circ \mathbf{$

A more quantitative description of this behaviour is obtained from the results of the least-squares fits. Owing to the difference in the integrated intensities between the $\frac{4}{5}$ 40 ferroelectric and the paraelectric Bragg reflections, the temperature dependence of the total integrated intensity $\overline{0}$ $\overline{0}$ 50 100 150 200 250 300 *(Figure 4a)* clearly shows the two phase transitions and **PRESSURE (MPa)** the hysteresis phenomena observed upon heating and cooling at constant pressure. Similarly, the pressure Figure 4 Total integrated intensity of the $(200+110)$ Bragg peaks dependence of the total intensity at constant temperature (ferroelectric and paraelectric) of the 7 dependence of the total intensity at constant temperature (ferroelectric and paraelectric) of the 70/30 copolymer: (a) *versus temperature* at 30 MPa for (\diamond) heating and (\diamond) cooling runs; shows the hysteresis of the ferroelectric transition: at (6) *versus* pressure at 410K for (\Diamond) decreasing and (\bullet) increasing (4) increasing (4) 410 K the copolymer is in the paraelectric phase at low pressure

 $\frac{a}{\text{[cooling]}}$ (*Figure 4b*). The total intensity is the same after temperature or pressure cycling and this demonstrates the reversibility of the phase transition and of the degree of crystallinity (after preliminary cycling³).

335, \approx ... The difference between the integrated intensities of the ferroelectric and the paraelectric phases can be partly attributed to different degrees of crystallinity in the two phases (the degree of crystallinity has been reported to $25/25$ be about 10% lower in the paraelectric phase³). But the $\frac{m}{1.55}$ main reason for this difference is a change in the neutron $\frac{m}{1.55}$ structure factor of the composite (200+110) Bragg 1.1 1.1 1.55 structure factor of the composite $(200+110)$ Bragg reflection. This is justified by the fact that a much smaller reflection. This is justified by the fact that a much smaller difference is observed in the X-ray structure factors³.
b Theorder to analyse these data in terms of yolu

b In order to analyse these data in terms of volume
 [[abstractions of the two phases we must first consider that fractions of the two phases we must first consider that out of the transition region, i.e. either in the homogeneous ferroelectric or paraelectric phase, the integrated intensity decreases almost linearly with increasing temperature or 430 $\frac{2430}{\frac{24$ for the reduction of the structure factor owing to thermal $T (K)$ $\left\{\begin{matrix} \begin{matrix} 1 & 1 \end{matrix} \end{matrix} \begin{matrix} 2 & 3 \end{matrix} \end{matrix} \begin{matrix} 3 & 4 \end{matrix} \begin{matrix} 4 & 6 \end{matrix} \end{matrix} \begin{matrix} 3 & 6 \end{matrix} \begin{matrix} 4 & 6 \end{matrix} \begin{matrix} 6 & 1 \end{matrix} \begin{matrix} 1 & 1$ For a given Bragg reflection the temperature factor B is $\overrightarrow{340}$ $\overrightarrow{1.1}$ proportional to the mean-square displacement of the Q ($\mathbf{\hat{A}}^{-1}$) atoms perpendicular to the Bragg planes, i.e. $B = 8\pi^2 \langle u_{\perp}^2 \rangle$, which increases with temperature and decreases with pressure. From the observed changes in the integrated

$$
\frac{\partial B}{\partial T} = \frac{8\pi^2}{Q^2} \left(\frac{1}{I} \frac{\partial I}{\partial T} \right)
$$

$$
\frac{\partial B}{\partial P} = \frac{8\pi^2}{Q^2} \left(\frac{1}{I} \frac{\partial I}{\partial P} \right)
$$

and
 $\frac{\partial B}{\partial P} = \frac{8\pi^2}{Q^2} \left(\frac{1}{I} \frac{\partial I}{\partial P} \right)$

According to our whole set of measurements under

isobaric or isothermal conditions we obtain
 $\partial B/\partial T = 0.13 \text{ Å}^2 \text{ K}^{-1}$ and $\partial B/\partial P = -0.024 \text{ Å}^2 \text{ MPa}^{-1}$

in isobaric or isothermal conditions we obtain $\frac{1}{2}$
 $\frac{\partial R}{\partial T} = 0.13 \frac{\mathring{A}}{\mathring{A}}^2 K^{-1}$ and $\frac{\partial R}{\partial P} = -0.024 \frac{\mathring{A}}{\mathring{A}}^2 M P_3^{-1}$...

$$
\partial B/\partial T = 0.13 \text{ Å}^2 \text{ K}^{-1} \text{ and } \partial B/\partial P = -0.024 \text{ Å}^2 \text{ MPa}^{-1}
$$

$$
\partial B/\partial T = 0.05 \,\text{\AA}^2 \,\text{K}^{-1}
$$
 and $\partial B/\partial P \approx 0$

in the ferroelectric phase.

Concerning the ferroelectric phase, one may remark [410K] that a linear extrapolation to 0 K gives $B = 15 \text{ Å}^2$ at room temperature, a value in good agreement with that $\sum_{\alpha=0}^{100}$ $\left\{ \begin{array}{ccc} -\alpha & -\alpha & -\alpha & -\alpha \\ \vdots & \vdots & \ddots & \vdots \\ \alpha & \alpha & \alpha & \beta\end{array} \right\}$ obtained from powder diffraction results at room $\overline{}$ \overline temperature¹⁵. The results obtained in the paraelectric phase are consistent with a higher disorder vanishing through a phase transition (well above $0 K$), and the effect of pressure on the Debye-Waller factor is attributed to $\begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix}$ 40 a higher compressibility of the lattice (see *Table 1*).

A more detailed insight into the phase transition • **20**
mechanism is obtained in considering the evolution of $\frac{3}{4}$ the volume fraction of each phase as deduced from the \geq 0 integrated intensity of each Bragg reflection (divided by $\frac{0}{0}$ 50 100 150 200 250 300
the Debye–Waller factor). The results plotted in *Figure 5a* PRESSURE(MPa) the Debye-Waller factor). The results plotted in *Figure 5a* show the transformations upon heating and cooling and show the transformations upon heating and cooling and Figure 5 Relative contents of the ferroelectric (F) and paraelectric (P)
the broad ranges of phase coexistence (of about 25 K and F_1) and F_2 and F_3 and F_4 the broad ranges of phase coexistence (of about 25 K and phases in the 70/30 copolyrner: (a) *versus* temperature at 30 MPa 15 K, respectively), as well as the extended temperature \Box F, \odot P) upon heating and \Box F, \odot P) upon cooling; (b) *versus* range of melting (and crystallization) characteristic of pressure at 410 K (\Box F, \bigcirc P) for decreasing pressure and (\blacksquare F, \lozenge P) for polymeric materials. Between the cooling and the heating increasing pressure runs a large hysteresis of about $40-50 \text{ K}$ is observed for the ferroelectric transition while a smaller hysteresis, 170/30 COPOLYMER of about 10K, is observed between melting and recrystallization. *Figure 5b* shows a similar behaviour for 500 the ferroelectric transition under pressure: for decreasing increasing pressure it extends only over 40 MPa, the hysteresis being about 120 MPa. Let us remark, however, that in this pressure scan the transition is not complete. $\frac{1}{2}$ **400**

pressure the transition extends over 60 MPa and for
increasing pressure it extends only over 40 MPa, the
hysteresis being about 120 MPa. Let us remark, however,
that in this pressure scan the transition is not complete.
F For such diffuse transitions there is no clear agreement in the literature of the definition of a mean transition \Box
temperature, except perhaps for the case of binary \Box 350 temperature, except perhaps for the case of binary mixtures for which the starting point, the end point, and the rate of transformation are thermodynamically well defined. In our case we have a spread of transition $300\begin{array}{ccc} 300 & 50 & 100 & 150 & 200 & 250 & 300 \\ 1 & 50 & 100 & 150 & 200 & 250 & 300 \end{array}$ temperatures which comes from the inhomogeneous **PRESSURE (MPa)** character of the material (distribution of size of the crystallites, inhomogeneities in comonomer compositions Figure 6 Phase diagram of the 70/30 copolymer showing the and atrain fields¹⁷. Such a system never reaches real ferroelectric and melting transitions: Curie temper and strain fields¹⁷). Such a system never reaches real $\binom{1}{2}$ and upon cooling (\Box); melting temperatures (\bullet) and crystallization thermodynamic equilibrium in a finite time and one temperatures (\odot) thermodynamic equilibrium in a finite time and one can only reduce the kinetic effects by using slow transformation rates. Even so, the volume fractions evolve smoothly without clear-cut starting points and From our experimental data, this last definition is
end points. The mean transition temperature could more precise and we have used it to draw the end points. The mean transition temperature could more precise and we have used it to draw the then be defined by the maximum transformation rate pressure-temperature phase diagram shown in Figure 6. corresponding to the inflection points of the volume

fractions and to the maximum of the specific heat behaviour is observed but at a correspondingly higher fractions and to the maximum of the specific heat anomaly; alternatively, it is also possible to define it as temperature. Therefore, the Curie temperature increases the midpoint of the transformation, i.e. as the temperature (both upon heating and cooling), suggesting greater for which the volume fraction of the transformed phase stability of the low temperature phase. This is what is is 50%. expected from the specific volume increase through the

pressure-temperature phase diagram shown in *Figure 6*.
Upon increasing pressure the same phase transition

ferroelectric transition^{3,17}. Similarly, the melting and the 70/30 COPOLYMER crystallization temperatures increase under pressure in 30 MPa crystallization temperatures increase under pressure in 30 **MPa** consistency with the fact that pressure favours the more 5 compact structure.

thermal hysteresis of the ferroelectric transition as
well as that of melting-crystallization remains almost
unchanged in the observed pressure range, although the
ferroelectric transition lines are not straight. From the well as that of melting-crystallization remains almost $\begin{array}{cc} \text{...} \\ \text{on} \\ \text{...} \end{array}$ unchanged in the observed pressure range, although the ferroelectric transition lines are not straight. From the $\overrightarrow{6}$ 4.6 slopes at low pressure $(< 100 MPa$) we obtain

$$
dT_{\rm C^{+}}/dP \approx dT_{\rm C^{-}}/dP = 0.38 \text{ K} \text{ MPa}^{-1}
$$

$$
dT_{\rm M}/dP \approx dT_{\rm v}/dP = 0.25 \text{ K} \text{ MPa}^{-1}
$$

indicating a clear decrease in the range of stability of the $T_{\text{EMPERATURE}}(K)$ paraelectric phase with increasing pressure. At higher pressures the slope of the ferroelectric transition lines decreases down to about 0.28 K MPa⁻¹ and thus a merging of the two transition lines could be expected
only at a much higher pressure.

dependence of the Curie Concerning the pressure.
 $\frac{1}{2}$ Concerning the pressure dependence of the Curie $\frac{1}{2}$ 4.8 apperature, the above values are close to those $\frac{1}{2}$ 4.8 oported by Samara¹¹ from dielectric temperature, the above values are close to those $\frac{1}{2}$ 4.7 the negative values are close to those $\frac{1}{2}$ 4.7 a 70/30 mol% copolymer $(dT_c/dP = 0.30 \pm 0.02 \text{ K} \text{ MPa}^{-1}$ $\qquad 4.6$ upon heating and cooling) and those reported by $\mathbb{R}_{\mathcal{A},\mathcal{B}}$ \mathcal{A},\mathcal{B} Akashige *et al.*¹² from X-ray diffraction on a 73/27 mol% v or \overline{I} \overline{I} or \overline{I} \overline{I} is a set of \overline{I} is a set of copolymer $(dT_c/dP \approx 0.35 \text{ K} \text{ MPa}^{-1})$. But concerning the $\frac{1}{2}$ 4.4 melting temperature, Samara¹¹ found a transition 4.3 line corresponding to $dT_M/dP \approx 0.5 \text{ K MPa}^{-1}$ (at low 0 50 100 150 200 250 300 pressure), a result which led him to conclude that the **PRESSURE (MPa)** pressure), a result which led him to conclude that the range of stability of the paraelectric phase increases under range of stability of the paraelectric phase increases under Figure 7 Ferroelectric (F) and paraelectric (P) $(200 + 110)$ d spacings pressure. Our results based on the vanishing of the incough the ferroelectric transition diffraction peaks through the melting point clearly disagree with his conclusions.

change of the unit cell parameters and this can be pressure observed in the temperature dependence of the d spacing of the composite $(200 + 110)$ Bragg reflection in the ferroelectric and paraelectric phases. Figure 7 displays the results at 30 MPa: upon heating the d spacing is broader perpendicular to the chain axis increases by 9% (in the $(20 \text{ K})^{3,17}$) perpendicular to the chain axis increases by 9% (in the $(20 \text{ K})^{3,17}$.
middle of the coexistence region), while $d_{0.01}$ (along the The change in the d spacings under hydrostatic pressure middle of the coexistence region), while d_{001} (along the chain axis direction) decreases by $10\%^5$. This results in

$$
(V_{\text{para}} - V_{\text{ferro}})/V_{\text{ferro}} = +6.7\%
$$
 $T_{\text{C}+} = 380 \text{ K}$

It is worth pointing out that upon cooling a smaller volume change is observed (owing to the different thermal *80/20 copolymer*

$$
(V_{\text{ferro}} - V_{\text{para}})/V_{\text{ferro}} = -4.9\%
$$
 $T_{\text{C}^-} = 342 \text{ K}$

Figure 7 also demonstrates that in the ferroelectric ferroelectric transition and the melting-crystallization phase ordinary thermal expansion is observed and that were then performed. At high pressure, upon cooling from phase ordinary thermal expansion is observed and that were then performed. At high pressure, upon cooling from the results obtained upon heating and cooling fall almost the melt, the conolymer crystallizes in the paraelect the results obtained upon heating and cooling fall almost the melt, the copolymer crystallizes in the paraelectric onto the same straight line over the whole range of phase (Figure δ) and further transforms into the onto the same straight line over the whole range of phase *(Figure 8)* and further transforms into the temperatures. On the contrary, in the paraelectric phase, ferroelectric phase. But, upon heating, the melting occurs temperatures. On the contrary, in the paraelectric phase, ferroelectric phase. But, upon heating, the melting occurs the behaviour of the lattice spacing appears to be different prior to complete transformation from the fe upon cooling and upon heating. Combined with the evolution of the volume fractions (*Figure 5a*), one can evolution of the volume fractions *(Figure 5a)*, one can For the profile fitting of these data it was found see that linear thermal expansion is observed *(with a* empirically that a single Lorentzian peak was sufficient see that linear thermal expansion is observed (with a empirically that a single Lorentzian peak was sufficient
rather large slope) when the volume fraction of the to describe the composite ferroelectric Bragg peak rather large slope) when the volume fraction of the to describe the composite ferroelectric Bragg peak paraelectric phase Φ_{para} is higher than 80%, while at the (200+110). The results of these fits provide first the paraelectric phase Φ_{para} is higher than 80%, while at the (200 + 110). The results of these fits provide first the first stages of its growth the paraelectric lattice is integrated intensities from which the volume f first stages of its growth the paraelectric lattice is integrated intensities from which the volume fractions of compressed. Indeed, the growth of this phase of higher the ferroelectric and paraelectric phases are calculat compressed. Indeed, the growth of this phase of higher the ferroelectric and paraelectric phases are calculated specific volume is somehow self-hindered inside the (after evaluation of the Debye–Waller factor). Figure 9 specific volume is somehow self-hindered inside the (after evaluation of the Debye-Waller factor). *Figure 9* ferroelectric matrix and this perhaps provides an displays the results obtained for low and high pressure

through the ferroelectric transition of the $\frac{70}{30}$ copolymer (the lines show the coexistence of the two phases and the arrows show the disagree with his conclusions, evolution): (a) *versus* temperature at 30 MPa (D F, © P) upon heating The ferroelectric transition is accompanied by a large \Box F, \Box P) upon cooling; (b) *versus* pressure at 410 K \Box F, \odot P) for increasing pressure and (\Box F, \Box P) for increasing

explanation of why the range of phase coexistence
is broader upon heating (40K) than upon cooling

chain axis direction) decreases by 10%⁵. This results in *(Figure 7b)* also allows an analysis of the lattice compressibility, which appears to be about 2.5 times compressibility, which appears to be about 2.5 times higher in the paraelectric phase than in the ferroelectric phase.

expansion coefficients of the two phases) In the copolymer with 20% TrFE the Curie temperature is very close to the melting point. Isobaric temperature scans (at eight different pressures) through both the prior to complete transformation from the ferroelectric
to the paraelectric phase.

displays the results obtained for low and high pressure.

Figure 8 Series of neutron powder diffractograms of the 80/20 Figure 8 Senes of neutron powder diffractograms of the $\frac{80}{20}$ into the α phase, as for copolymers of lower TrFE contents from 470 K to 410 K; (b) heating run from 410 K to 485 K at atmospheric pressure ¹⁸. from 470 K to 410 K; (b) heating run from 410 K to 485 K

heating and (\blacksquare F, \spadesuit P) upon cooling: (a) at 0.1 MPa; (b) at 250 MPa temperatures (\bigcirc)

80/20 COPOLYMER
250 MPa1 a **Example 250 MPa1** a **E 2** transition starts at around 370 K and is just complete
cooling at 415 K when melting of the paraelectric phase **a Example 12** at 415 K when melting of the paraelectric phase occurs. Thus the midpoints of these two successive transformations are only 19 K apart. Upon cooling at a rate of about 0.5 K min⁻¹ the crystallization of the paraelectric phase is observed 18 K below its melting 410 $\frac{1}{2}$ point, and this undercooling is noticeably higher than in
the 70/30 copolymer. Additionally, the ferroelectric $T (K)$ $\frac{1}{\sqrt{2}}$ $\frac{1}{\sqrt{2}}$ transition shows a large thermal hysteresis of almost 60 K.

 $470/$ ^{\sim} At high pressure (250 MPa) the transition points are $\overline{1.1}$ $\overline{1.55}$ shifted to higher temperatures and the Curie temperature $Q(\mathring{A}^{-1})$ gets closer to the melting point in such a way that the ferroelectric transition is no more complete upon heating. b This means that some ferroelectric crystallites melt without transforming into the paraelectric phase. Indeed, in the pressure-temperature phase diagram a triple point is expected above which a single line would correspond to the melting of the ferroelectric phase. The distribution of transition temperatures from one crystallite to another results therefore in a distribution of triple points. The **485** results in *Figure 8* show that about 30% of the crystallites have their triple points at a pressure lower than 250 MPa. $T (K)$ $\left\{ \begin{array}{c} \begin{array}{c} \begin{array}{c} \text{W(1)} \\ \text{W(2)} \end{array} \end{array} \end{array} \right\}$ Moreoever, upon cooling from the melt, the temperature $\frac{3}{1.1}$ range of the paraelectric phase shrinks under pressure. 1.55 It is then expected, from an extrapolation, that above
Q (\mathring{A}^{-1}) 500–600 MPa the 80/20 copolymer would no longer $500-600$ MPa the $80/20$ copolymer would no longer crystallize into the paraelectric phase but, very probably,

From the results obtained at different pressures a phase diagram can be drawn using the same convention as defined above for the midpoints of the transitions. Thus, **80/20 COPOLYMER** the transition lines represented in *Figure 10* describe the transition lines represented in *Figure 10* describe the behaviour of a 'middle crystallite' which transforms when behaviour of a 'middle crystallite' which transforms when 1 00 just 50% of the total volume has been transformed. In such a representation the ferroelectric transition line and $80 \left[\begin{array}{ccc} 7 & 7 & 7 \end{array} \right]$ the melting transition line should cross at a triple point when the maximum volume fraction of the paraelectric **blue becomes less than 50%. From an extrapolation of** the data obtained between 0.1 and 250 MPa this triple 40 $\begin{bmatrix} 1 & 0 \end{bmatrix}$ //1 and $\begin{bmatrix} 1 & 0 \end{bmatrix}$ with is estimated to be at $P^* \approx 500$ MPa and $T^* \approx 560$ K upon heating.

Figure 10 Phase diagram of the 80/20 copolymer showing the Figure 9 Relative contents of ferroelectric (F) and paraelectric (P) ferroelectric and melting transitions: Curie temperatures upon heating phases in the 80/20 copolymer *versus* temperature (\Box F, \odot P) upon (\Box) and upon cooling (\Box); melting temperatures (\bigcirc) and crystallization

the transition lines are not straight. Indeed, for the slopes [80/20 COPOLYMER] at low pressure $(< 100 \text{ MPa}$) one gets $[0.1 \text{ MPa}]$

$$
dT_{c+}/dP = 0.32
$$
 K MPa⁻¹

$$
dT_{\rm M}/dP = 0.27 \, {\rm K} \, {\rm MPa}^{-1}
$$

whose linear extrapolation would place the triple point
upon heating at $P^* \approx 350$ MPa.
In addition, for both transitions the thermal hysteresis $\begin{array}{c} 62 & 4.6 \\ \hline 24.5 & 4.5 \end{array}$ upon heating at $P^* \approx 350 \text{ MPa}$.

In addition, for both transitions the thermal hysteresis $\frac{60}{60}$ 4.5 appears to change with pressure: for the ferroelectric \overline{a} transition upon cooling one gets a higher slope at low σ 4.4

$$
1T_{\rm C}/dP = 0.36 \,\rm K \,MPa^{-1}
$$

but the two lines become almost parallel at high pressure, as for the $70/30$ copolymer. The thermal hysteresis of 1250 MPa the ferroelectric transition does not depend much on pressure that the contract of the contract of

$$
T_{\rm C^+} - T_{\rm C^-} \approx 50 \text{ K}
$$

Moreover, the difference between the melting and

stallization temperatures surprisingly increases with

essure, and this could be related to the fact that at high

essure the melting of the paraelectric phase coexists

t crystallization temperatures surprisingly increases with pressure, and this could be related to the fact that at high $\frac{1}{4}$, 6 pressure the melting of the paraelectric phase coexists $\frac{8}{60}$ 4.6 with the melting of the ferroelectric phase.

For this copolymer a larger volume change occurs σ 4.4 during the ferroelectric transition as can be seen in *Figure 11,* where the d spacing of the composite 4.3 $\frac{1}{375}$ 425 475 525 $(200 + 110)$ Bragg reflection is presented (at 0.1 MPa and TEMPERATURE (K) at 250 MPa). At atmospheric pressure the contraction (expansion) of the a and b lattice parameters through the Figure 11 Ferroelectric (F) and paraelectric (P) (200+110) d spacings
through the ferroelectric transition of the 80/20 copolymer versus transition reaches -8.8% upon cooling (and $+11.3\%$ upon heating). Thus the volume of the unit cell contracts (the lines show the coexistence of the two phases and the arrows show
by 7.6% upon cooling and expands by 10% upon heating.
the evolution: (a) at 0.1 MPa; (b) at 2 by 7.6% upon cooling and expands by 10% upon heating. As already mentioned for the 70/30 copolymer, such a large volume increase produces internal strains in the coexistence region. It is visible in *Figure 11* that, upon 60/40 COPOLYMER I a heating, the lattice spacing of the first nuclei of the paraelectric phase is compressed by about 0.8% with respect to its equilibrium value (measured at the same temperature upon cooling). This compressive strain, $3⁷$ which can be described by an internal pressure as high as 120 MPa, decreases as the paraelectric phase grows. At (external) atmospheric pressure, it almost vanishes when the paraelectric volume fraction is larger than 80% . $\qquad \qquad$ \qquad \qquad However, under high (external) pressure the maximum volume fraction of the paraelectric phase remains below $\frac{440}{1.1}$ 70%. The further volume increase owing to melting seems $\overline{1.1}$ 1.55 to maintain a noticeable internal pressure in the range to maintain a noticeable internal pressure in the range of coexistence of the two solid phases with the molten phase. This effect explains the upwards shift of the melting temperature with respect to the crystallization $\|\cdot\|$ **Integral in the integral integral in the integral in the integral integral in the integral integral in the integral integral integral integral integral inte** temperature and also the apparent triggering of the melting of the paraelectric phase by the melting of the ferroelectric phase *(Figure 9).*

60/40 copolymer

Owing to the complex phase transition behaviour of the 60/40 mol% copolymer at low pressure, we shall first $T(K)$ discuss the results obtained at high pressure.

At 300 MPa, the evolution of the composite Bragg $\overline{1.1}$ reflection $(200 + 110)$ through the ferroelectric transition $Q(\hat{A}^{-1})$ *(Figure 12)* is similar to that observed for the 70/30 mol% Figure 12 Series of neutron powder diffractograms of the 60/40 and the 80/20 mol% copolymers at low pressure. It is, copolymer at 300 MPa in the 0 range 11-1.55 however, worth noting that, in the phase transition region, from 440 K to 370 K ; (b) heating run from 370 K to 440 K

temperature (\Box F, \Diamond P) upon heating and (\blacksquare F, \spadesuit P) upon cooling

copolymer at 300 MPa in the Q range 1.1-1.55 \tilde{A}^{-1} : (a) cooling run

the Q separation between the low and the high $\frac{60}{40 \text{ COPOLYMER}}$
temperature Bragg peaks is less clear. This could be $\frac{300 \text{ MPa}}{300 \text{ MPa}}$ temperature Bragg peaks is less clear. This could be partly attributable to a smaller variation of the lattice parameters between the ferroelectric and the paraelectric 100 upon heating, the high temperature peak seems to arise phases 15, but it is also apparent from *Figure 12* that, as a shoulder on the ferroelectric peak. This effect is even more pronounced at low pressure *(Figure 13)*, where the $\overline{6}$ 60 high temperature peak seems to persist down to room $\begin{array}{cc}\n\bullet \\
\bullet \\
\bullet\n\end{array}$ 40

In order to describe this effect we have considered for $\overline{\mathbf{z}}$ 20 the fitting procedure a double Lorentzian $(L_{110} + L_{200})$ corresponding to the ferroelectric peak and another $\begin{array}{ccc}\n & \text{S} & \text{L} & \text{L} & \text{L} & \text{L} & \text{L} \\
\text{Lorentzian, which we shall call the 'disordered' peak,} & 350 & 370 & 390 & 410 \\
\text{corresponding to the evolution of the high temperature} & \text{TEMPERATURE (K)}\n\end{array}$ Lorentzian, which we shall call the 'disordered' peak, $\frac{350}{350}$ 370 390 410 430 450 corresponding to the evolution of the high temperature peak.

300 MPa *(Figure 14a)* are comparable to those obtained
with the two other copolymers, but the evolution of the $\frac{2}{4.8}$ with the two other copolymers, but the evolution of the
lattice parameter *(Figure 14b)* shows an anomalous
behaviour for the 'disordered phase'. When this phase
appears (around 380 K) the interchain distance of 4.65 Å
i behaviour for the 'disordered phase'. When this phase appears (around 380 K) the interchain distance of $\angle{4.65 \text{ Å}}$ $\angle{4.6}$ is small, but between 415 K and 430 K an increase of $\frac{8}{15}$ **4.5** about 1.7% is observed towards the expected d spacing \overline{a} \overline{b} \overline{a} 4.4 of the paraelectric phase. Upon cooling the same
behaviour is observed with a thermal hysteresis of 15 K ,
 4.3 s behaviour is observed with a thermal hysteresis of 15 K , $\qquad 4.3 \frac{\text{K}}{350}$ $\qquad 370$ $\qquad 390$ $\qquad 410$ $\qquad 430$ $\qquad 450$ noticeably smaller than that exhibited by the volume $\frac{350}{370} = \frac{390}{410} = 410$ fractions $(25 K)$.
These results suggest the existence of a phase $\frac{1}{2}$ Figure 14 Temperature dependence of the ferroelectric (F) and

These results suggest the existence of a phase transition between the paraelectric phase and another $\Box F, \triangle D$) upon heating and $(\Box F, \triangle D)$ upon cooling: (a) relative contents of each phase; (b) (200+110) d spacings 'low temperature disordered' (LTD) phase. Thus the d spacing given by the fitting procedure corresponds to an average between the paraelectric and the LTD phases. 160/40 COPOLYMER Alternatively, the diffraction data have also been analysed $\frac{1300 \text{ N}}{300 \text{ MPa}}$

from 380 K to 305 K; (b) heating run from 315 K to 390 K three different phase transitions occur.

the 'disordered' (D) phases of the 60/40 copolymer at 300 MPa

1.1 1.55 Figure 15 Relative contents of the ferroelectric (F), low temperature
 $\sqrt{Q} (\hat{A}^{-1})$ figure 15 Relative contents of the ferroelectric (F) phases of the 60/40 copolymer disordered (LTD) and paraelectric (P) phases of the 60/40 copolymer at 300 MPa *versus* temperature: $(\Box \nvdash, \Diamond \nightharpoonup \text{LTD}, \bigcirc \text{P})$ upon heating; \Box F, \triangle LTD, \Box P) upon cooling

considering three phases $(F, LTD$ and $P)$ whose d spacings obey linear thermal expansions, as represented by the straight lines in *Figure 14b*.

According to this description, the evolution of the three 390, **+** volume fractions is shown in *Figure 15.* Upon heating, up to 417 K, the decrease in the ferroelectric fraction $T (K)$ $\left|\frac{1}{K}\right|$ $\left|\frac{1}{K}\right|$ corresponds to the emergence of the LTD phase. Above 417K, both the LTD and the ferroelectric phases $315\sqrt{\frac{315}{1.1}}$ transform into the paraelectric phase. Upon cooling, the 1.55 transformation of the paraelectric phase gives rise to the $Q(\hat{A}^{-1})$ simultaneous appearance of the LTD and ferroelectric simultaneous appearance of the LTD and ferroelectric phases, but at lower temperatures only the ferroelectric Figure 13 Series of neutron powder diffractograms of the $60/40$ phase remains. Therefore, both upon heating and cooling, copolymer at 0.1 MPa in the Q range 1.1–1.55 Å⁻¹; (a) cooling run

temperature disordered (LTD) and paraelectric (P) phases of the 60/40 copolymer at 0.1 MPa (\Box F, \triangle LTD, \bigcirc P) upon heating and line, for which the volume fraction of the transformed (\Box F, \triangle LTD, \bigcirc P) upon cooling: (a) relative contents of each phase; phase is 50% (f (\blacksquare F, \blacktriangle LTD, \clubsuit P) upon cooling: (a) relative contents of each phase; (b) (200+110) *d* spacings

results at atmospheric pressure. Figure 16 shows the evolution of the volume fractions and the lattice parameters of each phase. As is also visible in *Figure 13*, the LTD phase persists down to room temperature and and its volume fraction seems to reach an equilibrium value (around 40-50%). This value, which clearly decreases with increasing pressure, actually depends on the thermal indicating an increase in the thermal hysteresis upon
history of the sample, showing the metastable nature of increasing pressure as absented by Algebra at 12 for history of the sample, showing the metastable nature of increasing pressure, as observed by Akashige *et al.*¹² for the LTD phase.

The evolution of the volume fractions is very similar upon heating and cooling with a hysteresis of only 7 K. In addition, the transformation of the paraelectric phase is very abrupt (over less than 10 K) and the growth of 4.6 the ferroelectric and LTD phases is nearly simultaneous. It is also worth noting that, upon heating, the ferroelectric phase partly transforms into the LTD phase, as already phase partly transforms into the LTD phase, as already $\overline{3}$ $\overline{4.5}$ \over

seen at high pressure.

The analysis of the ferroelectric d spacing under

pressure (*Figure 17*) shows that, whereas at high

pressure the evolution is consistent with the observed

compressibility of the 70/30 mol% cono The analysis of the ferroelectric d spacing under $\frac{6}{5}$
essure (Figure 17) shows that whereas at high $\frac{6}{5}$ 4.45 pressure (Figure 17) shows that, whereas at high pressure the evolution is consistent with the observed $\begin{array}{cc} \mathbf{5} \\ \mathbf{4.4} \end{array}$ compressibility of the 70/30mo1% copolymer, at low pressure there is an additional expansion. This expansion σ 4.35 $\frac{1}{2}$ 70/30 COPOLYMER is attributed to the coexistence of the ferroelectric and LTD phases and disappears after electrical poling, when **4.3** LTD phases and disappears after electrical poling, when $\begin{array}{ccc} 4.3 & . & . & . & . & . & . & . \\ 4.3 & . & . & . & . & . & . & . & . \\ 9 & . & . & . & . & . & . & . & . & . \\ 100 & 150 & 200 & 250 & 300 & . & . & . \end{array}$ only the ferroelectric phase is present¹⁵. This is analogous $\begin{array}{ccc} 0 & 50 & 100 & 150 & 200 \\ \text{to the behaviour observed when a large number of defects & & & & \text{PRESSURE (MPa)} \end{array}$ to the behaviour observed when a large number of defects are present in the crystalline regions¹⁹. Moreover, the small coherence length of the ferroelectric phase along d spacing at room temperature: $\left(\bullet\right)$ 60/40 copolymer; $\left(\bullet\right)$ 70/30 the chain axis¹⁵ suggests a lamellar substructure of copolymer

60/40 COPOLYMER alternating LTD and ferroelectric regions along the chain

0.1 MPa i axis direction. This could explain the simultaneous axis direction. This could explain the simultaneous a appearance of the two phases upon cooling from the

Our results demonstrate that, with decreasing pressure, $\begin{bmatrix} 1 & 1 \end{bmatrix}$ ferroelectric phase towards a close mixture of a
 $\begin{bmatrix} 1 & 1 \end{bmatrix}$ follows: $\begin{bmatrix} 1 & 1 \end{bmatrix}$ ferroelectric phase with a new phase (LTD) 'distorted' ferroelectric phase with a new phase (LTD), $\begin{bmatrix} 1 & 1 & 1 \ 1 & 1 & 1 \end{bmatrix}$ the fraction of which may change with temperature and pressure. From X-ray diffraction measurements on 20 $\left\{\left\{\right\}\right\}$ oriented specimens with low VDF contents, Tashiro *et al.*⁵ have considered a single, low temperature phase **0 , , , '** '/°' L A including a kind of micro-twinning along the chain 300 320 340 360 3 a 0 400 axis - the so-called 'cooled phase'. Our results show that, even with a comparable arrangement, the coexistence of two phases of different symmetries has to be taken into account

• In addition, the evolution of the volume fractions upon 4.9 $\frac{1}{2}$ or $\frac{1}{2}$ or $\frac{1}{2}$ or $\frac{1}{2}$ beating shows that some of the ferroelectric regions 4.8 $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ undergo a Curie transition while the rest of them -4.7 $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ transform first into the LTD phase and then into the paraelectric phase. Therefore a triple point is expected in 4.6 $\frac{1}{2}$ \cdots s $\frac{1}{2}$ $\frac{1}{2}$ \cdots s $\frac{1}{2}$ \cdots corresponding the pressure-temperature phase diagram, corresponding 4.5 $\frac{1}{2}$ to the crossing of the ferroelectric-LTD and the **• o** 4.4 LTD-paraelectric transition lines. From the results obtained at different pressures, the volume fraction of the $4.3 \frac{1}{300}$ 320 340 360 380 400 LTD phase does not reach more than 50%. Thus, **TEMPERATURE** (K) according to the criteria used for the midpoint of the transition, the triple point should not appear in the phase Figure 16 Temperature dependence of the ferroelectric (F), low diagram. It is thus only possible to define one transition to the ferroelectric (F), low diagram. It is thus only possible to define one transition paraelectric phase upon cooling) *(Figure 18).*

Probably owing to the metastable mixture of phases, the transition points are scattered and it is not possible to detect a curvature of the transition line. From the Following the same procedure, we can now discuss the evolution of the transition temperature we obtain

$$
dT_{C^{+}}/dP = 0.31 \text{ K MPa}^{-1}
$$

$$
dT_{C^{-}}/dP = 0.26 \text{ K MPa}^{-1}
$$

$$
dT_M/dP \approx dT_r/dP = 0.27 \text{ K} \text{ MPa}^{-1}
$$

the $54/46$ mol% copolymer.

Figure 17 Pressure dependence of the ferroelectric $(200+110)$

and on the ferroelectric-paraelectric phase transition, we do the chain axis direction for the three compared the measurements performed at a composition $80/20$, $70/30$ and $60/40$ mol%. have compared the measurements performed at a

Figure 18 Phase diagram of the $60/40$ copolymer showing the

of the (200 + 110) d spacing through the ferroelectric transition at 200 MPa for the three copolymers: $\left(\frac{m}{20}, \frac{m}{20}, \frac{m}{20}, \frac{m}{20}, \frac{m}{20}, \frac{m}{20}, \frac{m}{20}\right)$

DISCUSSION pressure of 200 MPa (for which the three copolymers
In external order to obtain a more detailed insight into the effect exhibit a clear ferroelectric transition). Figure 19 displays In order to obtain a more detailed insight into the effect α can be clear ferroelectric transition). *Figure 19* displays schematically the behaviour of the *d* spacing perpendicular of the copolymer composition on the crystalline structure schematically the behaviour of the aspacing perpendicular $\frac{1}{2}$ and on the ferroelectric percelectric phase transition we to the chain axis direction for the t

From the temperature dependence of the d spacing, the linear thermal expansion coefficients $\alpha_{L,F}$ and $\alpha_{L,P}$ can be determined for the ferroelectric and paraelectric 160/40 COPOLYMER[crystalline phases, respectively *(Table 1).* It appears that 500 \blacksquare with a thermal expansion about three times larger in the $,450$. The same parametectric phase than in the ferroelectric phase. Such a paraelectric phase than in the ferroelectric phase. Such a paraelectric phase is a paraelectric phase than in the ferroelectric phase. Such a p large values are characteristic of a highly disordered phase with large amplitude, anharmonic lattice vibrations. Along the chain axis direction the d_{001} lattice spacing is $400 \frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ determined by the length of the covalent bonds, and therefore the thermal expansion is almost zero²⁰. Thus, $\begin{array}{c} \text{350} \\ \text{350} \end{array}$ $\begin{array}{c} \text{if one assumes the same linear thermal expansion along} \\ \text{the a end is more accurate.} \end{array}$ the a and b axes, one obtains a volumetric expansion coefficient α_V for each phase given by $\alpha_V = 2\alpha_L$. The results ,,, ~ , , , , are given in *Table 1.* The expansion coefficients of the 3 1 1 0 0 1 5 0 2 0 0 2 5 0 3 0 0 1 5 0 μ LTD phase, for the 60/40 copolymer, are also given and pressure (MPa)

appear to be close to those of the paraelectric phase.
Similarly, the linear lattice compressibility perpendicular ferroelectric and melting transitions: Curie temperatures upon heating to the chain axis χ_L is deduced from the pressure (a) and upon cooling (\square); melting temperatures (\bullet) and crystallization dependence of the *d* (a) and upon cooling (\Box) ; melting temperatures (\bullet) and crystallization dependence of the d spacing. *Table 1* again shows temperatures (\bigcirc) and crystallization dependence of the difference between the three conolyme little difference between the three copolymers. The compressibility of the paraelectric phase is about 2.5 times larger than that of the ferroelectric phase, in agreement 5 r an oriented and polarized PVDF sample confirm an equal

4.8 4.7

4.8 \overline{a}

4.8 \overline{b}

4.6 \overline{a}

4.5 \overline{a}

4.5 \overline{b}

4. • -- much lower. For the homopolymer PVDF, Newman *et* ^{4.7} $d = \begin{bmatrix} -1.2.4.4.7 \end{bmatrix}$
 *al.*²¹ reported that $\chi_{001} = 0.015 \times 10^{-4} \text{ MPa}^{-1}$ in the β

phase and $\chi_{001} = 0.07 \times 10^{-4} \text{ MPa}^{-1}$ in the *n* phase We phase and $\chi_{001} = 0.07 \times 10^{-4} \text{ MPa}^{-1}$ in the α phase. We 4.5 $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ have used these values, as a first approximation, in σ **4.4** $\begin{bmatrix} 1 & -1 & -1 \\ -1 & -1 & -1 \end{bmatrix}$ determining the volumetric compressibilities χ_V of the ferroelectric and paraelectric phases of the copolymers. *4.3 Table 1* shows the results obtained using the expression

By comparing the compressibilities of these copolymers Figure 19 Schematic representation of the temperature dependence with those obtained for other crystalline polymers²², it of the $(200+110)$ d spacing through the ferroelectric transition at is clear that the compressib is very large and does not correspond to the general

Table 1 Linear and volumetric thermal expansion coefficients (α_L and α_V) and linear and volumetric compressibilities (χ_L and χ_V) of each crystalline phase of the three copolymers. The linear coefficients are measured perpendicular to the chain axis; the subscripts F, P and LTD stand for ferroelectric, paraelectric and low temperature disordered phase. All the values are normalized to 370 K and atmospheric pressure and correspond to the low pressure behaviour (below 150 MPa)

Parameter	80/20 copolymer	70/30 copolymer	60/40 copolymer
$10^4 \alpha_{L,F} (K^{-1})$	1.1	0.9	0.9
$10^4 \alpha_{L,P} (K^{-1})$	3.0	3.2	3.5
$10^4 \alpha_{L,LTD} (K^{-1})$			3
$10^4 \alpha_{V,F} (K^{-1})$	2.2°	1.8	1.8
$10^4 \alpha_{V,P} (K^{-1})$	6.0	6.4	7.0
$10^4 \alpha_{v, \rm{LTD}} (K^{-1})$			6
10^4 $\chi_{L,F}$ (MPa ⁻¹)	0.6	0.6	0.55
10^4 $\chi_{L,P}$ (MPa ⁻¹)	1.5	1.5	1.6
10^4 χ _{L,LTD} (MPa ⁻¹)			1.5
$10^4 \chi_{V,F} (MPa^{-1})$	1.2	1.2	1.1
$10^4 \chi_{V,P} (MPa^{-1})$	3.1	3.1	3.3
$10^4 \chi_{v, \rm{LTD}} (MPa^{-1})$			\sim 3

Parameter	80/20 copolymer	$70/30$ copolymer	$60/40$ copolymer
		Atmospheric pressure	
T_c^a (K)	404	362	338.5
dT_{C^+}/dP^b (K MPa ⁻¹)	0.32	0.38	0.31
$\Delta V/V^c$ (%)	10	6.7	
ΔH^d (J g ⁻¹)	65	33	$\overline{}$
ΔS^e (J g ⁻¹ K ⁻¹)	0.16	0.09	
		200 MPa	
T_c (K)	467.5	430	397
dT_{C^+}/dP (K MPa ⁻¹)	0.27	0.25	0.31
$\Delta V/V$ (%)	9.9	6.6	1.5
ΔH (J g ⁻¹)	87	57	10
ΔS (J g ⁻¹ K ⁻¹)	0.19	0.13	0.025

Table 2 Summary of the important thermodynamic parameters for the ferroelectric transition upon increasing temperature at atmospheric pressure and at 200 MPa

^a Curie temperature

b Curie temperature change with pressure

c Relative volume change at the Curie temperature

d Enthalpy change of the crystalline phase at the transition

e Entropy change of the crystalline phase at the transition

disordered phases II and IV of poly(tetrafluoroethylene) increasing the TrFE content.

Moreover, for the paraelectric phase, the d spacing is actually non-linear and should be represented by a P is the external pressure and V is the volume. Thus, the second-order polynomial. The second-order terms are enthalpy change at the transition can be expressed second-order polynomial. The second-order terms are enthalpy change at the transition can be expressed $-1.1 \times 10^{-7} \text{ MPa}^{-2}$ and $-1.2 \times 10^{-7} \text{ MPa}^{-2}$, respect- as $\Delta H = (U_{\text{para}} - U_{\text{ferro}}) + P(V_{\text{para}} - V_{\text{ferro}})$. At atmos ively, for the 80/20 and 60/40 mol% copolymers. These pressure, the second term is negligible (around 5×10^{-3})

with composition, while the ferroelectric d spacing 0.9 J g^{-1} for the 60/40 copolymer. These values are not, increases drastically with increasing TrFE content. however, sufficient to account for the increase in th Therefore the discontinuous change of the unit cell enthalpy change ΔH under pressure. This means that the volume at the Curie temperature (T_C) , which amounts to change in the internal energy $U_{para} - U_{ferro}$, volume at the Curie temperature (T_c) , which amounts to change in the internal energy $U_{para} - U_{ferro}$, which 10% in the 80/20 copolymer, drops to 6.7% for the 70/30 corresponds to the entropy change at constant volume, 10% in the 80/20 copolymer, drops to 6.7% for the 70/30 corresponds to the entropy change at constant volume, copolymer (Table 2). This means that the first-order also increases with inreasing pressure. In fact, from copolymer *(Table 2)*. This means that the first-order also increases with inreasing pressure. In fact, from character of the ferroelectric transition decreases when Table 2 it appears that the whole entropy change character of the ferroelectric transition decreases when *Table 2* it appears that the whole entropy change increasing the TrFE content. Correspondingly, the $\Delta S = S_{\text{para}} - S_{\text{ferro}}$ also increases with pressure. As an range of phase coexistence decrease - two effects which with pressure seems physically unreasonable, one must are clearly related to the nucleation and growth of the conclude that it is the entropy of the ferroelectric phase new phase in a matrix of different volume. It is also worth which decreases with increasing pressure.
noting that the volume change at T_c is insensitive to Let us remark here that a statistical analysis of noting that the volume change at T_c is insensitive to hydrostatic pressure, while the transition temperature

These two results can be analysed using the

$$
\frac{\mathrm{d}T_{\mathrm{C}}}{\mathrm{d}P} = T_{\mathrm{C}} \frac{\Delta V}{\Delta H}
$$

which allows the enthalpy change of the crystalline phase. ΔH (and the entropy change $\Delta S = \Delta H/T_c$) to be calculated Indeed, an analysis of the composition effect shows at the transition temperature, using the phase diagrams that both ΔH and ΔS decrease with increasing qu at the transition temperature, using the phase diagrams that both ΔH and ΔS decrease with increasing quantities of *Figures 6, 10* and 18. The results obtained upon heating, of TrFE. From an entropic point of view, at atmospheric pressure and at 200 MPa, are given in an increase in the ferroelectric entropy, a result in Table 2. They show a significant increase in ΔH agreement with the observation of increasing disorder in (and ΔS) with increasing pressure (from $\Delta H = 33 \text{ J g}^{-1}$ to the ferroelectric structure, which becomes metas range 0.1 to 200 MPa). Furthermore, a large drop in

behaviour. Such high values are only observed for the the enthalpy and entropy changes is observed when disordered phases II and IV of poly(tetrafluoroethylene) increasing the TrFE content.

(PTFE) $(1.89 \times 10^{-4} \text{ MPa}^{-1}$ and $2.5 \times 10^{-4} \text{ MPa}^{-1}$, In analysing the effect of pressure on the enthalpy respectively).
Moreover, for the paraelectric phase, the d spacing is is given by $H = U + PV$, where U is the internal energy. -1.1×10^{-7} MPa⁻² and -1.2×10^{-7} MPa⁻², respect- as $\Delta H = (U_{\text{para}} - U_{\text{ferro}}) + P(V_{\text{para}} - V_{\text{ferro}})$. At atmospheric values are also larger than those of most other polymers Jg^{-1} . However, at high pressures, this term is partly and are comparable only with those of PTFE²². responsible for the enthalpy increase. For example, and are comparable only with those of $PTFE^{22}$. responsible for the enthalpy increase. For example, An important result which is clearly visible from at 200 MPa $P(V_{\text{para}}-V_{\text{terro}}) = 10.5 \text{ J g}^{-1}$ for the 80/20 *Figure 19* is that the paraelectric d spacing changes little copolymer, 6.9 J g⁻¹ for the 70/30 copolymer and however, sufficient to account for the increase in the increasing the TrFE content. Correspondingly, the $\Delta S = S_{\text{para}} - S_{\text{ferro}}$ also increases with pressure. As an thermal hysteresis of the transition and the temperature increase m the entropy of the paraelectric phase

hydrostatic pressure, while the transition temperature the conformationally disordered paraelectric phase²³ increases rapidly with pressure.
gives a conformational entropy of the order of R ln 2, i.e. gives a conformational entropy of the order of R In 2, i.e. 0.084 J $g^{-1} K^{-1}$. This value corresponds to the increase Clausius-Clapeyron relation in entropy, at constant volume, from a ferroelectric phase without conformational disorder. Thus, a comparison with the results of *Table 2* reveals both the increase in ΔS associated with the volume change at T_c and the decrease in ΔS owing to the partial disorder of the ferroelectric phase.

> of TrFE. From an entropic point of view, this implies agreement with the observation of increasing disorder in with respect to the LTD phase for the $60/40 \text{ mol\%}$ copolymer¹⁵.

In the present paper we have described the structural We are grateful to the ILL staff for technical support properties of the ferroelectric and paraelectric crystalline and especially to P. Convert. J. Pannetier. J. Torre properties of the ferroelectric and paraelectric crystalline and especially to P. Convert, J. Pannetier, J. Torregrossa,

phases of the P(VDF–TrFE) copolymers. P. Andant and L. Melesi for their kind assistance. It is a

From neutron diffraction measurements as a function pleasure to acknowledge Professor J. Lajzerowicz for of temperature and pressure, we have been able to fruitful discussions. The samples were kindly supplied by determine the thermodynamic parameters characteristic of the crystalline phases alone, of their structural phase transitions and of their melting. The results obtained at atmospheric pressure and at high pressure for three copolymers allow us to conclude that the structure and REFERENCES the entropy of the ferroelectric phase are much more influenced by the composition and by the external 1 Wang, T. T., Herbert, J. M. and Glass, A. M. 'The Applications' pressure than those of the paraelectric phase. The increase 2
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unit cell and an increase in the entropy of the ferroelectric 4 Lovinger, A. J., Davis, G. T., Furukawa, T. and Broadhurst, unit cell and an increase in the entropy of the ferroelectric 4 Lovinger, A. J., Davis, G. T., Furulation and Broadhurst, This increasing disorder amplifies the effect of M. G. Macromolecules 1982, 15, 323 structure. This increasing disorder amplifies the effect of 5 decreasing dipolar energy in the lowering of the Curie temperature.

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Indeed, for the 80/20 copolymer, the temperature *Polym. Phys. Jpn* 1985, 28, 427
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crystallites undergo the ferroelectric transition prior to 12 Akashige. E., Taki, S., Horjuchi, T., Takemura, T. a crystallites undergo the ferroelectric transition prior to 12 Akashige, E., Taki, S., Horiuchi, T., Takemura, T. and melting.

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16 Bevington, P. R. 'Data Reduction and Error Analysis for the

16 Bevington, P. R. 'Data Reduction and Error Analysis for the

16 Bevington, P. R. 'Data Reduction and E This new phase interpenetrates the ferroelectric crystallites, producing a distortion of the ferroelectric lattice. Under 17 producing a distortion of the ferroelectric lattice. Under 17 Legrand, J. F., Lajzerowicz, J., Berge, B., Delzenne, P., pressure, the proportion of the ferroelectric phase Macchi, F., Bourgaux, C., Wicker, A. and Kruger, J. K. increases at the expense of the LTD phase which *Ferroelectrics* 1988,78, 151 Increases at the expense of the LTD phase which
almost disappears at about 300 MPa. Further structural 19 Lovinger, A. J., Davis, D. D., Cais, R. E. and Kometani, J. M.
studies of this new phase are recommended, especially studies of this new phase are recommended, especially
to determine whether the paraelectric-LTD phase 20 Delzenne, P. PhD Thesis, Grenoble University, France, 1986 to determine whether the paraelectric-LTD phase 20 Delzenne, P. PhD Thesis, Grenoble University, France, 1986
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CONCLUSION ACKNOWLEDGEMENTS

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